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**Thermophysical Properties of Energetic Ionic Liquids/Nitric Acid Mixtures:  
Insights from Molecular Dynamics Simulations**

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**Abstract**

Molecular dynamics (MD) simulations of mixtures of the room temperature ionic liquids (ILs) 1-butyl-4-methyl imidazolium [BMIM]/dicyanoamide [DCA] and [BMIM][NO<sub>3</sub><sup>-</sup>] with HNO<sub>3</sub> have been performed utilizing the polarizable, quantum chemistry based APPLE&P® potential. Experimentally it has been observed that [BMIM][DCA] exhibits hypergolic behavior when mixed with HNO<sub>3</sub> while [BMIM][NO<sub>3</sub><sup>-</sup>] does not. The structural, thermodynamic and transport properties of the IL/HNO<sub>3</sub> mixtures have been determined from equilibrium MD simulations over the entire composition range (pure IL to pure HNO<sub>3</sub>) based on bulk simulations. Additional (non-equilibrium) simulations of the composition profile for IL/HNO<sub>3</sub> interfaces as a function of time have been utilized to estimate the composition dependent mutual diffusion coefficients for the mixtures. The latter have been employed in continuum-level simulations in order to examine the nature (composition and width) of the IL/HNO<sub>3</sub> interfaces on the millisecond time scale.

## I. Introduction

There is increasing interest in use of room temperature ionic liquids (ILs) as fuels and propellants. Particularly enticing is the fact that RTILs have negligible vapor pressure, making them intrinsically much safer than traditional high vapor pressure and toxic fuels such as hydrazine. While most IL fuels are not hypergolic (i.e., do not spontaneously combust) when mixed with a liquid oxidizer (e.g., nitric acid), there is a number of energetic ILs that do exhibit hypergolicity.<sup>1</sup> Amongst these are 1-butyl-4-methyl imidazolium [BMIM]/dicyanoamide [DCA], shown in Figure 1. While [BMIM][DCA] when mixed with  $\text{HNO}_3$  is hypergolic, [BMIM][ $\text{NO}_3^-$ ] is not.<sup>2,3</sup> Understanding the behavior of any hypergolic system is very challenging and complicated due to the large manifold of reactions involved and the complex interplay between thermophysical properties and chemical kinetics. When a fuel droplet comes in contact with an oxidizer, some initial mixing is followed by the exothermic pre-ignition reactions that begin to decompose both fuel and oxidizer, producing various gaseous products. The pathways for these reactions involve highly reactive transient species that are difficult to detect experimentally. Changes in temperature and species concentrations due to these reactions as well as the underlying chemical kinetics themselves are also strongly dependent on physical factors that determine heat and mass transfer in these systems. Thermophysical properties such as enthalpy of mixing, species inter-diffusion, and thermal conductivity can all play an important role in controlling energy dissipation during the pre-ignition reaction stage.<sup>2,4</sup>

While thermophysical and transport properties of [BMIM][DCA] and [BMIM][ $\text{NO}_3^-$ ] have been investigated both experimentally<sup>5-10</sup> and from MD simulations,<sup>11-18</sup> there are no data available about thermophysical properties of these liquids mixed with  $\text{HNO}_3$ . Taking into account that it usually takes multiple milliseconds for ignition to occur in a hypergolic system there is a significant

(from a molecular scale point of view) time period when thermodynamic and thermophysical processes are dominating the behavior of the mixture and influence the kinetics of initial reactions. Therefore, we have carried out atomistic molecular dynamics (MD) simulations of  $\text{HNO}_3$ /[BMIM][DCA] and  $\text{HNO}_3$ /[BMIM][ $\text{NO}_3^-$ ] mixtures for the purposes of better quantifying the thermophysical properties of these mixtures with the ultimate aim of understanding the nature of hypergolicity in ILs. Furthermore, modeling of  $\text{HNO}_3$ /[BMIM][DCA], whether at the continuum level or at the level of detailed liquid-phase reaction pathways, will benefit greatly from an improved understanding of the thermodynamics, structure and transport properties of the mixture.

## II. Force Field and Simulation Methodology

MD simulations was performed using the polarizable APPLE&P® force field that has been developed and extensively validated on a variety of substances including ILs<sup>19</sup> and slightly modified for application to the specific ILs studied here.<sup>11</sup> Using this force field our previous simulations showed very good agreement with experimental thermophysical data for pure [BMIM][DCA] and [BMIM][ $\text{NO}_3^-$ ] RTILs.<sup>11</sup> For the current study the force field for  $\text{HNO}_3$  was obtained using our standard procedure, which considered all non-bonded interactions and the dipole polarizability of all atoms to be as transferred from previously calculated quantities for the nitrate anion, while bond, angular, and dihedral interactions were fit from *ab initio* data obtained at the MP2//aug-cc-pvDz level. Specific details about our fitting procedure can be found in Ref. [19] while the complete set of force field parameters is available free of charge upon signing a user license agreement.

MD simulations of bulk [BMIM][ $\text{NO}_3^-$ ]/ $\text{HNO}_3$  and [BMIM][DCA]/ $\text{HNO}_3$  mixtures have been conducted at 333 K and atmospheric pressure using cubic simulation cell (see Fig. 1). Systems with a composition ranging from 0.0 to 1.0 mol fraction IL in steps of 0.2 have been simulated. The pure  $\text{HNO}_3$  system contained 512 molecules while the mixed systems employed 600, 560, 512, or 468

total molecules in order of increasing IL mol fraction. Pure IL data was taken from the previous work, which employed 150 ionic pairs.<sup>11</sup> For the mixed systems, the number of ionic pairs employed were 100, 160, 192, and 208 for the mole fractions studied in increasing IL concentration. MD simulations were conducted using the molecular simulation package Lucretius which has the capability to handle polarization effects. Covalent bond lengths were constrained using the velocity-Verlet form of the SHAKE algorithm.<sup>20</sup> The Ewald summation method was used for treatment of long-range electrostatic forces between partial atomic charges and between partial charges and induced dipoles. A tapering function was used to drive the induced dipole/induced dipole interactions to zero at the cutoff of 10 Å, with scaling starting at 9.3 Å. (The form of the tapering function is given in the Supporting Information) Induced dipoles were calculated *via* a direct iteration with a predictor corrector method. A cutoff of 10 Å was used for all van der Waals interactions and the real part of electrostatic interactions in the Ewald summation. A multiple time step reversible reference system propagator algorithm<sup>21</sup> was employed. A time step of 0.5 fs was used for bonding, bending, dihedral, and out-of-plane deformation motions, while a 1.5 fs time step was used for non-bonded interactions within cutoff radius of 6.0 Å. Finally, the non-bonded interactions in the range between 6.0 and 10.0 Å and reciprocal part of electrostatic interactions were updated every 3 fs. Each system was initially equilibrated in the NPT ensemble for at least 1 ns, while production runs ranged from 120 to 180 ns depending on the system and temperature. The length of the production run was chosen to be long enough to allow molecules to reach a diffusive regime (when the ion mean squared displacement shows a linear time dependence,  $MSD(t) \sim t$ ), therefore allowing an accurate estimation of the self-diffusion coefficients.

In addition to equilibrium bulk simulations of IL/HNO<sub>3</sub> mixtures described above we also conducted MD simulations at non-equilibrium conditions in which we monitor the process of intermixing of IL and HNO<sub>3</sub> liquids. To conduct these simulations a liquid-liquid interface has to be set up as also shown in Figure 1 where RTIL and oxidizer are well separated. Several adjustments

to the simulation protocol have been implemented to allow these types of simulations. First, since IL and oxidizer are miscible the preparation of initial configuration that allows sharp yet tight (no vacuum) interface between IL and oxidizer has to be prepared. To create a sharp liquid-liquid interface we modify parameters for van der Waals interactions between IL and oxidizer molecules to make them more repulsive. Specifically, we set dispersion parameters  $C_{ij}$  (of the term  $-C_{ij}/r^6$ ) to zero for all cross-terms interactions between the IL and oxidizer. This simple modification was enough to provide a sharp interface between liquids without creating any additional artifacts to bulk materials away from the interface. Using this approach, initial configurations can be equilibrated for any period of time and then switched to simulations with realistic force field for production runs sampling the intermixing rate. In these simulations, the simulation cell dimensions were 35 X 35 X 140 Å with the larger dimension being perpendicular to the interface. Systems contained approximately the same volume of IL and oxidizer. During these simulations the pressure (stress tensor) was controlled separately in each direction, allowing the simulation to account for changes in pressure associated with mixing of the components. Simulations were conducted at 333 K and atmospheric pressure control along the large dimension (perpendicular to the interface). Two other dimensions were fixed at 35x35.

### **III. Simulations of Bulk Mixtures**

#### **A. Structure**

We began our analysis of the  $\text{HNO}_3/\text{IL}$  mixtures by investigating liquid-phase structure as a function of mixture composition. Figures 2a-b show center-of-mass BMIM-BMIM radial distribution functions  $g(r)$  as a function of separation  $r$  for  $\text{HNO}_3/[\text{BMIM}][\text{DCA}]$  and  $\text{HNO}_3/[\text{BMIM}][\text{NO}_3^-]$  mixtures for the various compositions investigated. It can be seen that for both systems there is a tendency for non-ideal mixing, i.e., the structure of the solution depends somewhat upon composition. For both mixtures the position of the first peak in the BMIM-BMIM

$g(r)$  moves to greater separation with increasing dilution (by  $\text{HNO}_3$ ). For  $\text{HNO}_3/[\text{BMIM}][\text{DCA}]$  the magnitude of the first peak also decreases with increasing dilution. The behavior observed in Figure 2 might be associated with strong  $\text{BMIM-HNO}_3$  interactions, but Figure 3, which show the  $\text{BMIM-HNO}_3$  radial distribution functions for the two mixtures at selected compositions, indicate that this is not the case. For the  $\text{HNO}_3/[\text{BMIM}][\text{DCA}]$  mixtures a slight decrease (as opposed to an expected increase) in the magnitude of the first peak in the  $\text{BMIM-HNO}_3$  radial distribution function with dilution by  $\text{HNO}_3$  can be seen. Both mixtures show near ideal mixing behavior with respect to  $\text{BMIM-HNO}_3$  interactions, i.e., very little composition dependence is observed in the radial distribution functions.

We have also investigated the role of  $\text{HNO}_3$  on interactions between cations and anions in the mixtures by examining the cation-anion radial distribution functions as shown Figures 4a,b for  $\text{HNO}_3/[\text{BMIM}][\text{DCA}]$  and  $\text{HNO}_3/[\text{BMIM}][\text{NO}_3^-]$ , respectively. The latter shows remarkably little influence of the oxidizer on cation-anion correlation in  $[\text{BMIM}][\text{NO}_3^-]$ , while the former indicates that introduction of  $\text{HNO}_3$  promotes stronger nearest-neighbor (first radial distribution function peak) interaction between  $\text{BMIM}$  and  $\text{DCA}$ . Examination of the anion-oxidizer radial distribution functions, shown in Figures 5, shows very little dependence of the nature of the  $\text{DCA/HNO}_3$  interaction on composition, while  $\text{NO}_3^-/\text{HNO}_3$  interactions become somewhat stronger with increasing dilution. These effects are manifested in  $\text{DCA-DCA}$  pair distribution functions that are essentially independent of composition while  $\text{NO}_3^-/\text{NO}_3^-$  correlations decrease notably with increasing  $\text{HNO}_3$  content, as shown in Figures 6a-b.

From the magnitude of the first peaks in the radial distribution functions, it is clear that the oxidizer interacts more strongly with the anions ( $\text{DCA}$  or  $\text{NO}_3^-$ ) than with the  $\text{BMIM}$  cation. Interestingly the first peak in the  $\text{HNO}_3/\text{NO}_3^-$  radial distribution function is high and narrow, indicating a strong preference for specific distance and/or orientations, while that for  $\text{HNO}_3/\text{DCA}$  is

quite broad, indicating less structure in this interaction. Atomically, the preferred interaction between  $\text{HNO}_3$  and  $\text{NO}_3^-$  is between the acidic proton and the oxygen atoms of the anion, while for  $\text{HNO}_3$  and DCA the preferred interaction is between the acidic proton and the (terminal) nitrogen atoms of the cyano groups. The H(acidic)-O(anion) and H(acidic)-N(cyano) atomic radial distribution functions are shown in Figure 7. Interestingly, remarkably little dependence of these interactions on the composition of the solution is observed. All radial distribution functions show a sharp, high peak at a separation of around two Å. We note that the force field employed in the simulations does not allow for transfer of the proton between species, so the nature of this interaction (e.g., minimum energy position/radial distribution function peak position) is driven entirely by physical (van der Waals and electrostatic) interactions. Integration of the radial distribution functions and multiplication by the appropriate densities yields the running coordination number of acidic protons near O(anion) or N(cyano) as shown in Figure 7c. We take a separation of 2.9 Å (see Figures 7a-b) as corresponding to the first coordination shell of acidic protons near O(anion) or N(cyano). As expected, the number of acidic hydrogen atoms coordinating each O(anion) or N(cyano) increases with increasing dilution. For the  $X_{\text{IL}} = 0.2$  solutions (80 mol%  $\text{HNO}_3$ ) the  $\text{NO}_3^-$  oxygen atoms and DCA cyano nitrogen atoms are fully coordinated, i.e., there is more than one on average of acidic hydrogen atoms in the first coordination shell of these atoms.

## B. Density, Volume of Mixing and Heat of Mixing

The density and excess volume for the two  $\text{HNO}_3$ /IL mixtures from simulations are shown in Figures 8a-b as a function of composition. The density of the pure ionic liquids are 1.030 g/cm<sup>3</sup> and 1.137 g/cm<sup>3</sup> for [BMIM][DCA] and [BMIM][NO<sub>3</sub>], respectively. These values are in a good agreement with experimental values of 1.041 g/cm<sup>3</sup> for [BMIM][DCA]<sup>6</sup> and 1.131 g/cm<sup>3</sup> for [BMIM][NO<sub>3</sub>]<sup>7</sup> with 0.5% and 1.1% deviation, respectively. The simulated density of the pure  $\text{HNO}_3$



at 298 K is 1.45 g/cm<sup>3</sup>, compared with an experimental density<sup>22</sup> of 1.51 g/cm<sup>3</sup>. Mixing of the ILs with increasing concentration of oxidizer results in a monotonic increase in density. Examination of the excess volume of mixing shows minimal deviation from ideal mixing behavior, particularly for the HNO<sub>3</sub>/[BMIM][NO<sub>3</sub><sup>-</sup>] system. Figure 8c shows the enthalpy of mixing as a function of composition for both IL mixtures. Both exhibit exothermic behavior, with the HNO<sub>3</sub>/[BMIM][NO<sub>3</sub><sup>-</sup>] system showing stronger exothermic character. Combined with the near-ideal entropy of mixing (configurational entropy) behavior revealed by the intermolecular radial distribution functions above, we can anticipate that both of these ILs are consoluble with HNO<sub>3</sub>. It is also clear that the temperature of the systems will increase upon adiabatic mixing, which is an important (if not crucial) aspect for onset of ignition in hypergolic mixtures. The extent of adiabatic heating for these mixtures is addressed in Section IV.

### C. Self-diffusion Coefficients

The rate at which a liquid fuel and oxidizer intermix is important in determining the hypergolic character of the mixture. While intermixing dynamics are investigated in more detail below, it is instructive to examine the self-diffusion coefficients of the IL components and the oxidizer as a function of mixture composition as shown in Figure 9. Figure 9 reveals that ion self-diffusion rates are significantly greater in [BMIM][DCA] than in the [BMIM][NO<sub>3</sub><sup>-</sup>], consistent with the relative viscosities of these ILs with [BMIM][NO<sub>3</sub><sup>-</sup>] being about factor 4 more viscous than [BMIM][DCA] at 333K.<sup>6,23</sup> The HNO<sub>3</sub> liquid has a much lower viscosity/greater self-diffusion coefficient than the ILs, hence, dilution of the ILs with HNO<sub>3</sub> results in a monotonic increase in ion self-diffusion coefficients and monotonic decrease in HNO<sub>3</sub> diffusion coefficient. The composition dependence of the ion and HNO<sub>3</sub> diffusion coefficients is greater in the HNO<sub>3</sub>/[BMIM][NO<sub>3</sub><sup>-</sup>] mixture than observed in HNO<sub>3</sub>/[BMIM][DCA] mixture. To first order this is consistent with the greater

difference in self-diffusion coefficients of  $\text{HNO}_3$  (fast) compared to the IL (slow) in the former system compared to the latter.

#### IV. Simulation of Ionic Liquid/Oxidizer Mixing

In addition to analysis of bulk properties under equilibrium conditions discussed above we have investigated properties of mixtures during the mixing process. Below we discuss the analysis of interdiffusion and adiabatic heating processes upon mixing.

##### A. Diffusion

Fig. 10a shows the concentration profile for  $\text{HNO}_3$  and the IL the  $\text{HNO}_3/[\text{BMIM}][\text{DCA}]$  system after 200 ps of mixing and after 3.5 ns of mixing, while Fig. 10b shows the composition profile after the same periods. Similarly, Fig. 11a shows the concentration profile for  $\text{HNO}_3$  and the IL the  $\text{HNO}_3/[\text{BMIM}][\text{NO}_3^-]$  system after 200 ps of mixing, after 3.0 ns of mixing and after 5.9 ns of mixing, while Fig. 11b shows the composition profile after the same periods. Each profile is an average of three profiles (e.g., the 200 ps profiles are averages of profiles at 100 ps, 200 ps and 300 ps). Examination of Figs. 10 and 11 show obvious asymmetry in mixing at the interface, indicating that the mutual diffusion coefficient  $D_{AB}$  ( $A = \text{oxidizer}$ ,  $B = \text{IL}$ ) is strongly composition dependent for both mixtures. A typical diffusion coefficient in these mixtures might be on the order of  $1 \times 10^{-9} \text{ m}^2/\text{s}$  (see Fig. 9), implying mixing on a nanometer length scale on a nanosecond time scale, consistent with behavior observed in Figs. 10 and 11.

The governing equation for mutual diffusion (Fick's second law) in one spatial dimension is given as<sup>24</sup>

$$\frac{\partial c_A(r,t)}{\partial t} = \frac{1}{r^m} \frac{\partial}{\partial r} \left( r^m D_{AB}(X_A) \frac{\partial c_A(r,t)}{\partial r} \right) \quad (1)$$

$$\frac{\partial c_B(r,t)}{\partial t} = \frac{I}{r^m} \frac{\partial}{\partial r} \left( r^m D_{AB}(X_A) \frac{\partial c_B(r,t)}{\partial r} \right) \quad (2)$$

$$X_A = \frac{c_A(r,t)}{c_A(r,t) + c_B(r,t)} \quad (3)$$

where  $m = 0$  for the slab geometry and 2 for spherical geometry. The dependence of  $D_{AB}$  on composition is a priori unknown and there is no robust theory for predicting  $D_{AB}(X_A)$ . However, it has been observed that the following relationship

$$\log D_{AB} = \log D_B + X_A (\log D_A - \log D_B) \quad (4)$$

where  $D_A$  and  $D_B$  are the pure component self-diffusion coefficients works well in some materials. Note that the self-diffusion coefficients of the species in the mixtures tend to follow (at least reasonably) this relationship (see Fig. 9). Using the profiles at 200 ps as initial conditions, we employed eqs. 1-4 to predict the concentration and composition profiles for both mixtures. Comparisons can be seen in Figs. 10 and 11, indicating that eq. 4 provides a reasonable description of the composition dependence of  $D_{AB}$ . Here we took the self-diffusion coefficient of pure  $\text{HNO}_3$  from Figure 9 and used the average of the cation and anion self-diffusion coefficients for the pure IL self-diffusion coefficients, again taken from Figure 9.

Once the composition dependence of the mutual diffusion coefficient is known, it is possible to utilize eqs. 1-4 with suitable initial and boundary conditions to prediction the concentration/composition profiles for any geometry of interest after any time of interest. For example, Fig. 12 shows the interfacial composition for a 2.5 mm radius droplet of  $[\text{BMIM}][\text{DCA}]$  and  $[\text{BMIM}][\text{NO}_3^-]$ , respectively, in a sea of  $\text{HNO}_3$  oxidizer, after periods of 10 and 100 ms. For both mixtures the interfacial region is on the order of microns in thickness as expected given the magnitude of the mutual diffusion coefficient (eq. 4). It is notable that on these time scales the width of the interfacial region is not significantly larger for the  $\text{HNO}_3/[\text{BMIM}][\text{DCA}]$  mixture than

for the  $\text{HNO}_3/[\text{BMIM}][\text{NO}_3^-]$  mixture, despite the fact that the self-diffusion coefficient for  $[\text{BMIM}][\text{DCA}]$  is almost four times greater than that for  $[\text{BMIM}][\text{NO}_3^-]$ . However, if we utilize an imaginary “fast” oxidizer with a self-diffusion coefficient four times that of  $\text{HNO}_3$ , mixing with  $[\text{BMIM}][\text{NO}_3^-]$  on these time scales occurs much more rapidly, as shown in Figure 12.

## B. Adiabatic Heating

Heat generation upon mixing is another important property that can influence kinetics of initial reactions and, hence, the hypergolicity of the mixture. Two approaches were applied for calculating heat generation due to mixing. First, calculations were based on bulk mixture heat of mixing data (see Section III.B). If one knows the heat of mixing for the mixture of two components (i.e., IL and oxidizer) then the heat generated upon their mixing can be estimated knowing the final composition of the mixture. For example, for the  $[\text{BMIM}][\text{DCA}]/\text{HNO}_3$  system with composition used in non-equilibrium simulations ( $X_{\text{IL}} = 0.23$ ) we estimate about 17 degrees temperature increase. For  $[\text{BMIM}][\text{NO}_3]/\text{HNO}_3$  with similar composition the corresponding heating is estimated to be about 45 degrees.

Alternatively one can conduct brute force simulations of mixing process in the NVE ensemble and directly measure how much the system heats up. While conceptually this method is straightforward, special care must be taken to control the integration uncertainty, which can otherwise lead to additional heat generation due to Hamiltonian drift. The latter can be measured by conducting simulations of a completely mixed state using the same simulation set up/parameters as in production run. A relatively short run (300-500ps) provides a good estimate of the rate of the Hamiltonian drift (if any) that can be then taken into account (subtracted) in the analysis of the production mixing simulation. Using this approach and applying correction for the Hamiltonian drift, a 17 degree heating was obtained from the non-equilibrium simulation of  $[\text{BMIM}][\text{DCA}]/\text{HNO}_3$  mixing, consistent with the estimate from bulk simulations discussed above.

Similarly, the heating in [BMIM][NO<sub>3</sub>]/HNO<sub>3</sub> system was found to be 45 degrees which is also consistent with the estimate from bulk simulations.

These simulations/estimations of heat generation due to physical mixing show that the heating is modest. In principle, taking into account that HNO<sub>3</sub> vaporization temperature is 353 K then even 20-40 degrees heating can be important. However, it is important to realize that the relatively narrow intermixing region is surrounded by the large amount of pure IL and oxidizer phases that can serve as heat sinks. In this case, the heating of the mixed layer will strongly depend on the interplay between thermal and molecular diffusivities in the system. The latter can be characterized by the Lewis number (Le) and is the ratio of the thermal diffusivity of a fluid, given as  $\alpha = \kappa / (C_p \rho)$ , to the molecular diffusivity. Taking into account typical values for thermal conductivity ( $\kappa$ ), heat capacity ( $C_p$ ), and density ( $\rho$ ) reported in the literature for IL<sup>25</sup> and nitric acid<sup>26</sup> we can estimate  $\alpha$  for our mixture components. The thermal diffusivity of nitric acid is around  $9 \times 10^{-8}$  m<sup>2</sup>/s, while that for a number of various ILs is in the range of  $6 \times 10^{-8}$  m<sup>2</sup>/s. Hence, unlike molecular (mutual or self) diffusivity, we anticipate that the thermal diffusivity of the ionic liquid/nitric acid mixture will not depend strongly on composition, and will be on the order of  $6 \times 10^{-8}$  m<sup>2</sup>/s. Using a representative diffusion coefficient of the IL/nitric mixtures of  $1 \times 10^{-9}$  m<sup>2</sup>/s (which is on the high side of the range), we estimate  $Le \geq 60$ . Hence, for viscous fluids such as ILs investigated here, the time scale of thermal diffusion is much less than that of mass diffusion. Even for nitric acid itself we estimate  $Le \sim 10$ .

This analysis indicates that it is unlikely that any noticeable local temperature rise can be expected in the interfacial region due to heat of mixing. In our brute force mixing simulations we have analyzed the local temperature profile after 200-500ps. On these time scales, IL and HNO<sub>3</sub> have only intermixed in a relatively small region of 2nm wide. If the thermal dissipation would be much slower than molecular diffusion then we should observe an increase of temperature in the

intermixed region due to heat of mixing. However, neither of two mixtures showed any indication of increased temperature in the intermixed region compared to the rest of the system, indicating that the thermal energy generated due to mixing quickly dissipates to IL and  $\text{HNO}_3$  phases and results in homogeneous heating of the entire system.

## V. Conclusions

Atomistic molecular dynamics simulations of  $\text{HNO}_3/[\text{BMIM}][\text{NO}_3^-]$  and  $\text{HNO}_3/[\text{BMIM}][\text{DCA}]$  mixtures using polarizable force field revealed a complete consolubility for both systems in the entire range of concentrations. Both mixtures exhibited exothermic behavior, with the  $\text{HNO}_3/[\text{BMIM}][\text{NO}_3^-]$  system showing stronger exothermic character. Analysis of various pair correlations functions showed very little dependence on mixture composition indicating a near-ideal entropy of mixing. Analysis of the liquid structure revealed that the most prominent difference between two mixtures is in the anion- $\text{HNO}_3$  correlations. The first peak in the  $\text{HNO}_3/\text{NO}_3^-$  radial distribution function is high and narrow, indicating a strong preference for specific distance and/or orientations, while that for  $\text{HNO}_3/\text{DCA}$  is quite broad, indicating less structure in this interaction. However, in both systems the potential anion proton acceptor atoms (oxygen for  $\text{NO}_3^-$  and nitrogens in DCA) are well coordinated by acidic hydrogen at all investigated compositions indicating that there no structural hindrances for initial anion protonation reactions to occur.

Analysis of molecular diffusivity showed a significant speed up of mobility of ions upon dilution with nitric acid. We found that molecular interdiffusion obtained from brute force simulation of mixing IL and oxidizer can be accurately described by a simple diffusion equation utilizing parameters obtained from MD simulations and simple empirical relation for calculation of mutual diffusion coefficients. The developed continuum level analytical model allowed us to estimate concentration profiles on time and length scales relevant to hypergolic ignition (multiple

ms and  $\mu\text{m}$ ) but are well outside of accessibility range for brute force atomistic MD simulations. Our analysis indicates that despite quite different diffusivity/viscosity between two investigated ILs their intermixing with nitric acid is quite similar on time scales of 10-100ms. Finally, the analysis of adiabatic heating upon mixing IL and oxidizer revealed that the released enthalpy of mixing is sufficient to allow a noticeable heating in the intermixed region. However, due to intrinsically high thermal diffusivity (compared to molecular diffusivity) of IL and nitric acid all heat generated in the intermixed layer is quickly dissipating to non-mixed regions. Taking into account that on time scales 10-100ms only a small fraction of a fuel droplet has intermixed with an oxidizer and hence the dominating non-mixed regions of IL and oxidizer can quickly sink the heat generated in the intermixed region. Therefore, no noticeable temperature increase due to heat of mixing can be expected in the intermixing region.

## **VI. Acknowledgment**

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### Figure Captions.

Figure 1. Chemical structure of ions and nitric acid as well as snapshots from equilibrium bulk simulation and non-equilibrium mixing simulation of [BMIM][DCA]/nitric acid system.

Figure 2. BMIM-BMIM radial distribution functions for  $\text{HNO}_3$ /[BMIM][DCA] (a) and  $\text{HNO}_3$ /[BMIM][ $\text{NO}_3^-$ ] (b) mixtures.

Figure 3. BMIM- $\text{HNO}_3$  radial distribution functions for  $\text{HNO}_3$ /[BMIM][DCA] and  $\text{HNO}_3$ /[BMIM][ $\text{NO}_3^-$ ] mixtures at selected compositions.

Figure 4. Cation-anion radial distribution functions for  $\text{HNO}_3$ /[BMIM][DCA] (a) and  $\text{HNO}_3$ /[BMIM][ $\text{NO}_3^-$ ] (b) mixtures.

Figure 5. Anion- $\text{HNO}_3$  radial distribution functions for  $\text{HNO}_3$ /[BMIM][DCA] and  $\text{HNO}_3$ /[BMIM][ $\text{NO}_3^-$ ] mixtures at selected compositions.

Figure 6. Anion-anion radial distribution functions for  $\text{HNO}_3$ /[BMIM][DCA] (a) and  $\text{HNO}_3$ /[BMIM][ $\text{NO}_3^-$ ] (b) mixtures.

Figure 7. The H(acidic)-O(anion) and H(acidic)-N(cyano) atomic radial distribution functions for  $\text{HNO}_3$ /[BMIM][ $\text{NO}_3^-$ ] (a) and  $\text{HNO}_3$ /[BMIM][DCA] (b), along with the corresponding running coordination numbers (c).

Figure 8. Density (a), excess volume (b) and heat of mixing (c) for  $\text{HNO}_3$ /[BMIM][DCA] and  $\text{HNO}_3$ /[BMIM][ $\text{NO}_3^-$ ] mixtures as a function of composition.

Figure 9. Ion and oxidizer self-diffusion coefficients as a function of mixture composition for  $\text{HNO}_3$ /[BMIM][DCA] and  $\text{HNO}_3$ /[BMIM][ $\text{NO}_3^-$ ] mixtures.

Figure 10. Time-dependent composition (a) and concentration (b) profiles for the  $\text{HNO}_3$ /[BMIM][DCA] slab system after 200 ps and 3.5 ns of mixing.

Figure 11. Time-dependent composition (a) and concentration (b) profiles for the  $\text{HNO}_3$ /[BMIM][ $\text{NO}_3^-$ ] slab system after 200 ps, 3.0 ns and 5.9 ns of mixing.

Figure 12. Interfacial profiles for a 2.5 mm radius sphere of [BMIM][DCA] or [BMIM][ $\text{NO}_3^-$ ] (indicated by arrows) in a sea of  $\text{HNO}_3$  predicted by using eqs. 1-4. The “fast” oxidizer system shows mixing of [BMIM][ $\text{NO}_3^-$ ] with an oxidizer than has a self-diffusion coefficient four times that of  $\text{HNO}_3$ .

Figure 1.

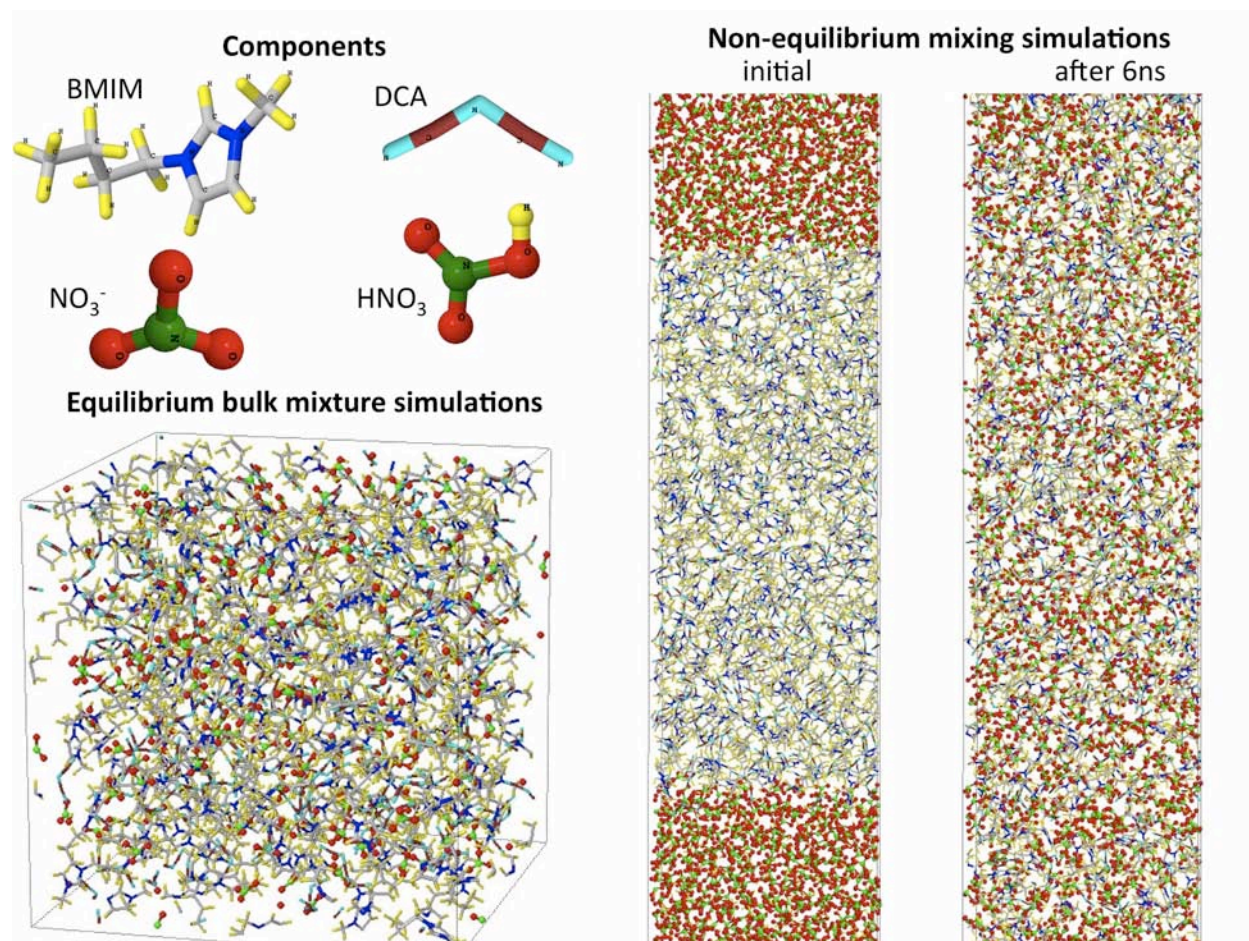


Figure 2.

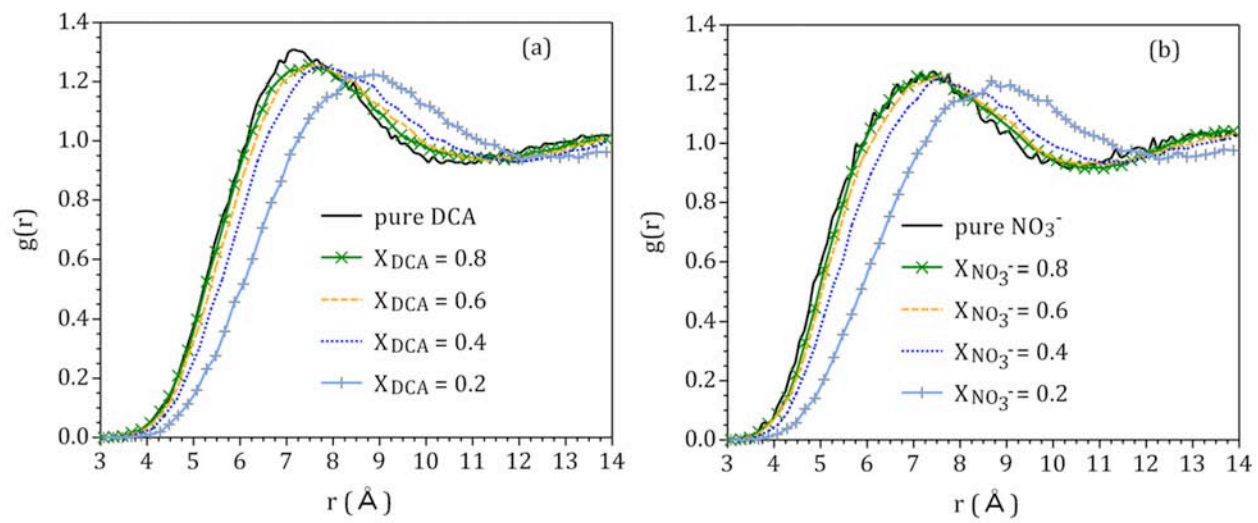


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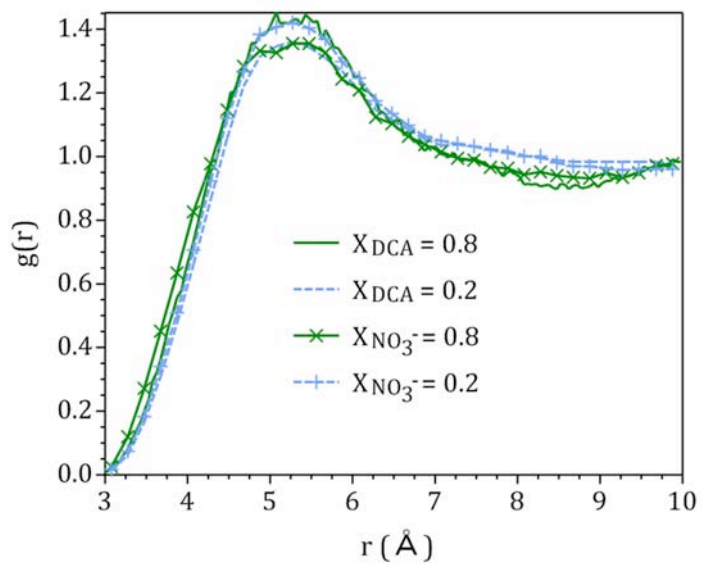


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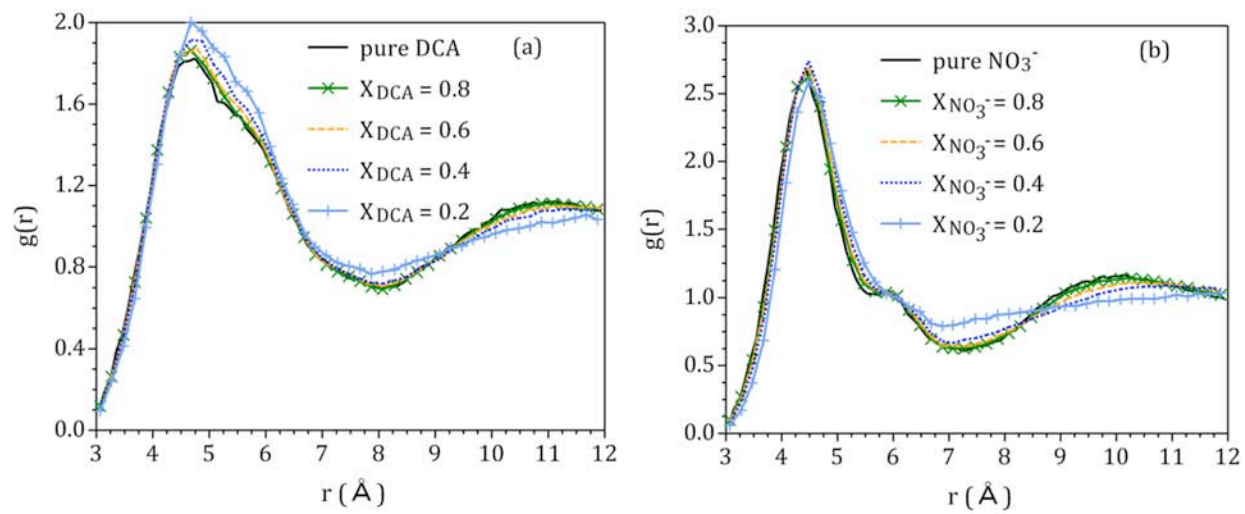


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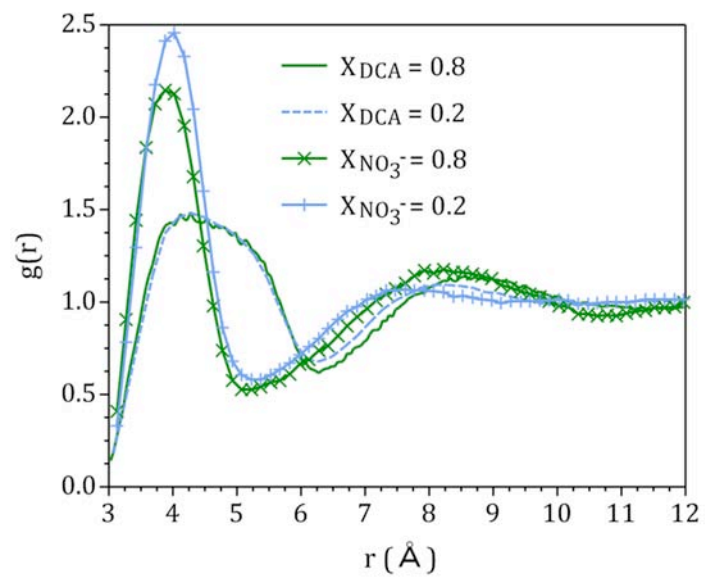




Figure 6.

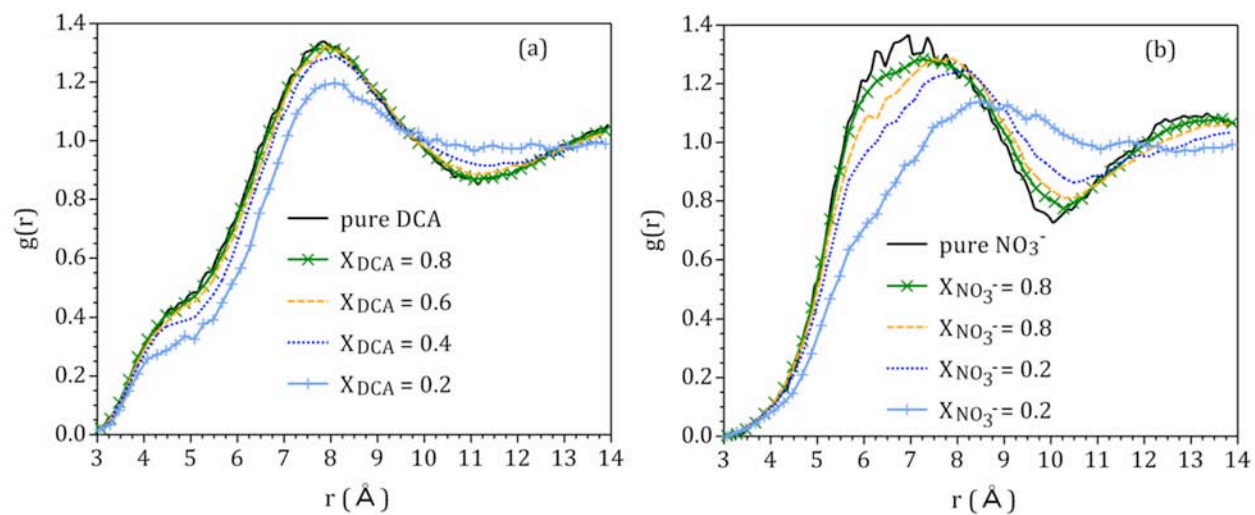


Figure 7

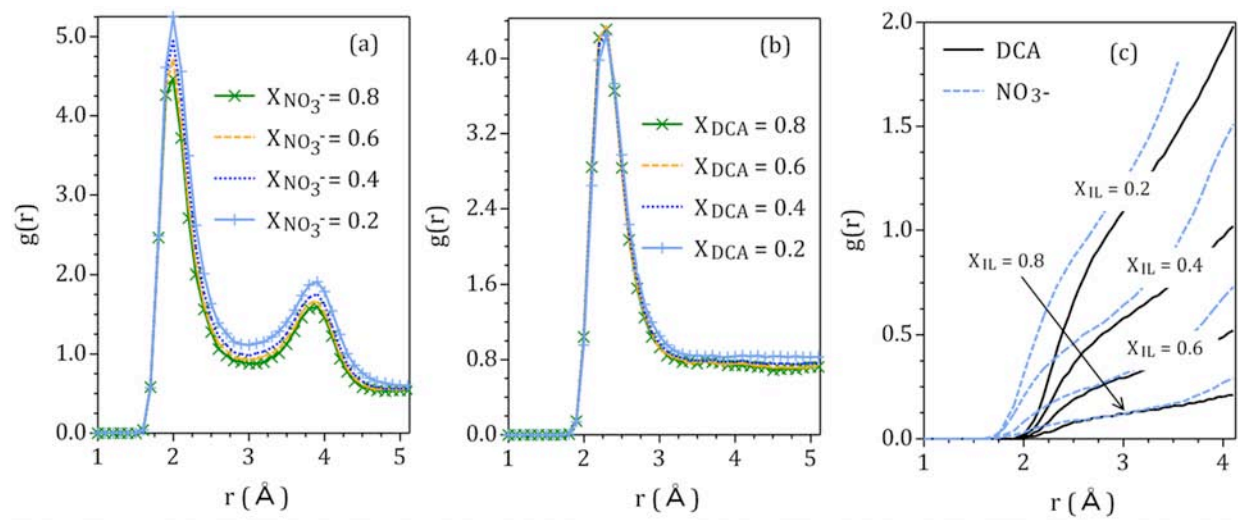


Figure 8

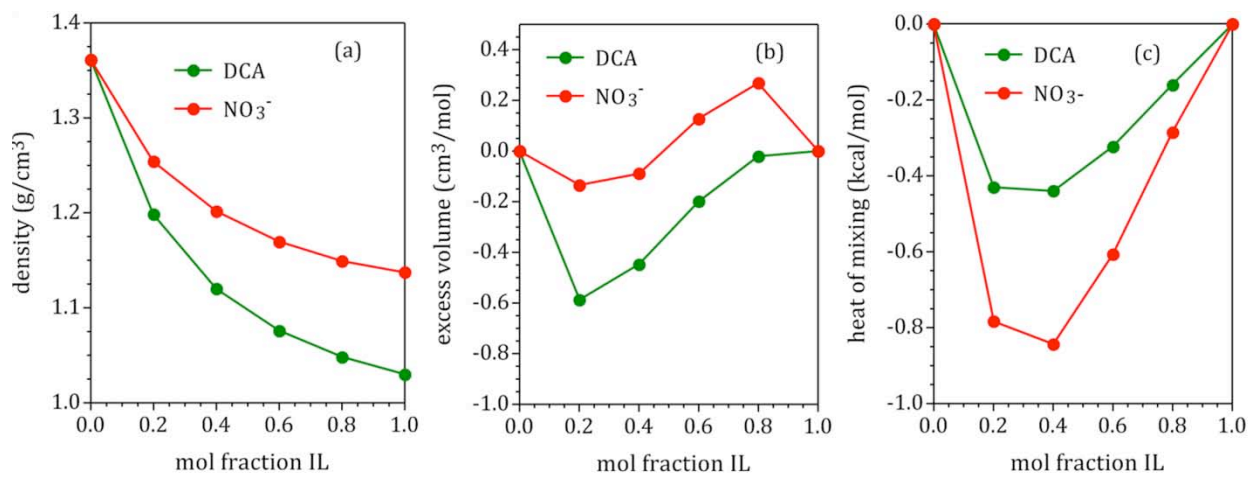


Figure 9.

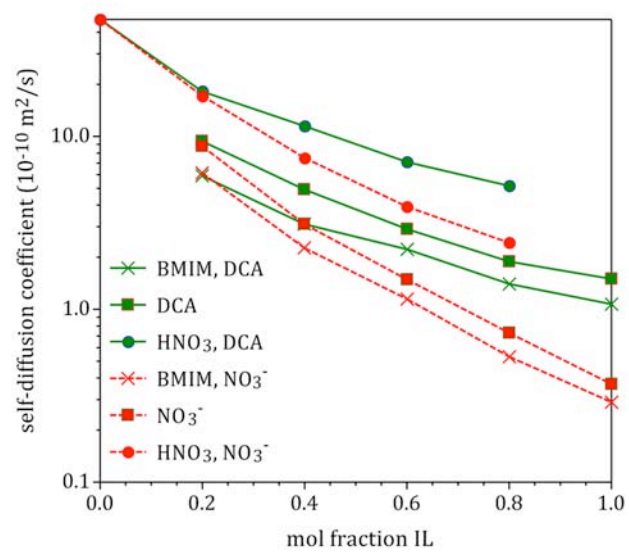


Figure 10.

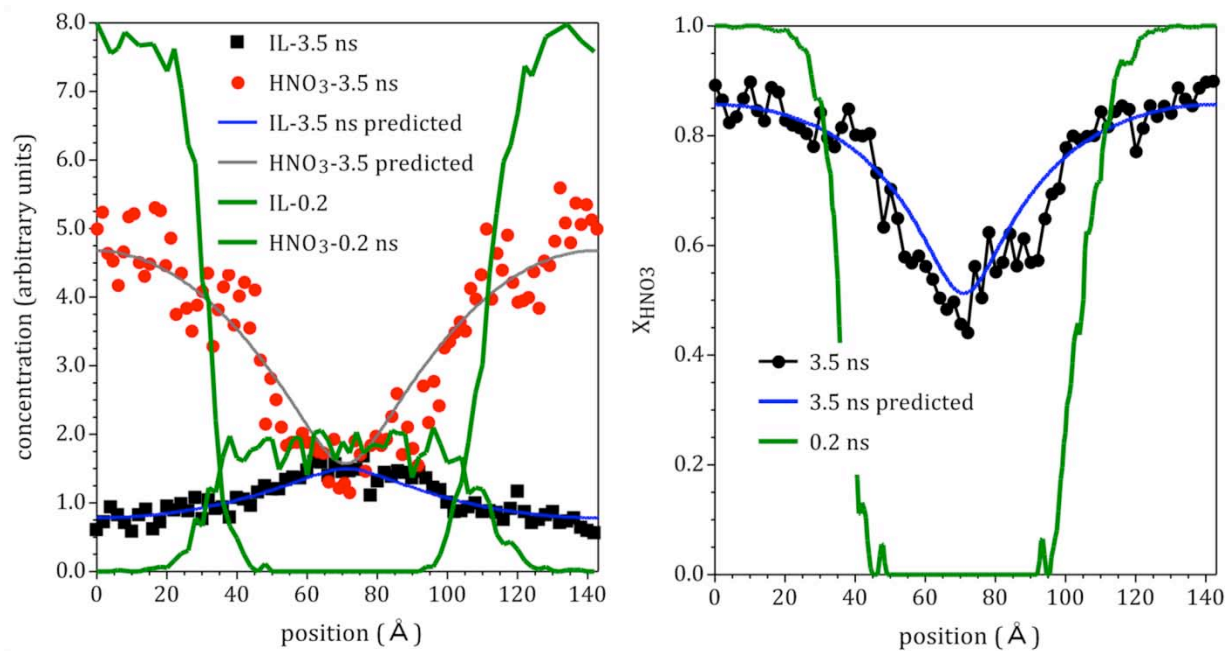


Figure 11.

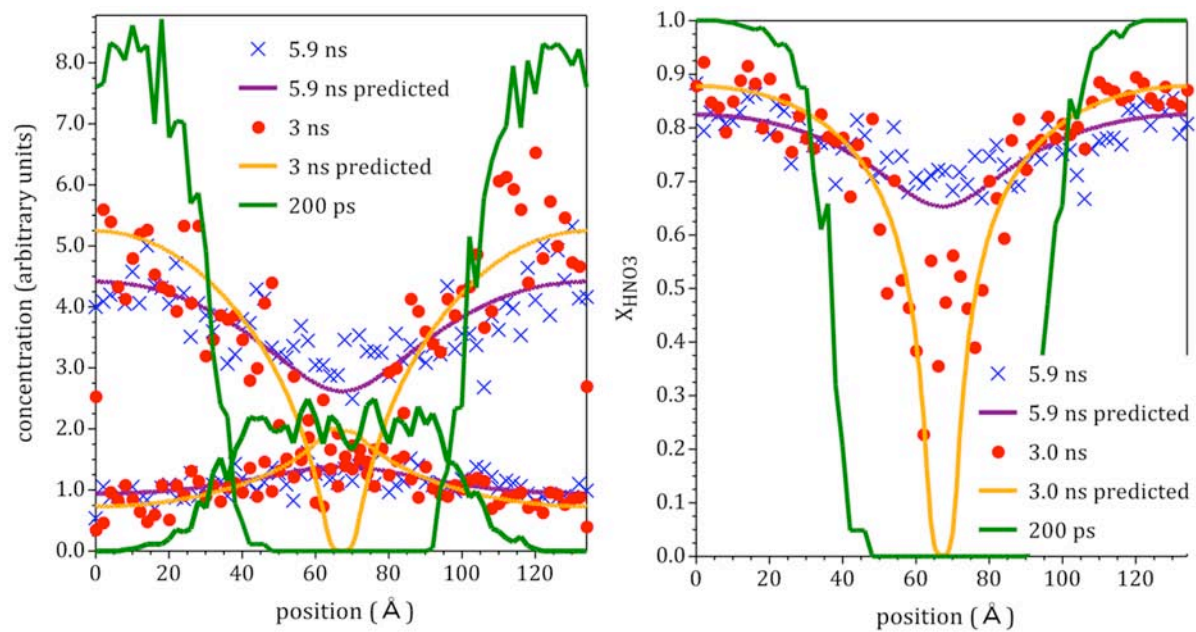


Figure 12.

